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# MRL-JAYA: A FUSION OF MRLDE AND JAYA ALGORITHM

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**Abstract** Jaya algorithm is a newly developed metahueristics algorithm to solve optimization problems. In this paper we have proposed a new variant named MRL-Jaya which is a fusion of Jaya algorithms with modified random localization based DE (MRLDE) algorithm. MRL-Jaya connects two algorithms by a systematic approach to utilize the advantage of both in a single variant. MRL-Jaya has tested on 13 traditional and 6 shifted benchmark problems taken from literature. In last the result and comparison shows the efficiency of proposed variant.

Keyword: Optimization, Differential evolution Algorithm, Jaya Algorithm.

# 1 Introduction

A lot of problems occur in various sciences and engineering filed can be modelled as global optimization problems. Use of traditional nonlinear programming techniques may show to be ineffective for solving such problems because of the occurrence of non linearity, non continuity, non differentiability and multiple local/global optima. In recent years, many non-traditional and nature inspired based methods have been developed in the area of optimization. Some of the well-known non-traditional techniques are GA, ACO, DE, PSO, ABC, TLBA, Jaya Algorithm and so on. Differential Evolution (DE) algorithm is first proposed by Storn and Price in [1]. The advantage of DE is including ease of implement, reliable, robust and efficient optimization algorithm. The compact design and the use of fewer control parameters make it more popular. However it does not guarantees to converge to optimum always. So many researches have been carried out on its improved versions and applications in different fields during some last years. Some popular enhanced variants of DE are, JDE [2], ODE [3], SaDE [4], jADE [5], LeDE [6], and so on. Some other DE variants which have developed recently can be found in literature given in [7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21]. A well organized literature review of DE algorithm with full details can also be found in [22, 23, 24]. MRLDE is an enhanced variant of DE algorithm proposed by Kumar and Pant [25] in 2012. It is based on modified mutation strategy in which base vector is selected in a strategic mode to pick up the performance of algorithm. The significance of MRLDE in optimization problems of various engineering and science can be found in [26, 27, 28, 29]. Jaya algorithm is newly developed metaheuristics algorithm in the field of optimization. It is proposed by Rao [30] in 2015. Like DE, It is also a gradient-free and population based search technique which repeatedly modified the solutions. The main advantage of the algorithm is its compact design and ease to use. Due to this reason it has become quite popular rapidly in solving many real life optimization problems. Some of recently developed Jaya algorithms variants and its applications are given in [31, 32, 33, 34, 35, 36, 37, 38, 39, 40] In this paper, a new variant named MRL-Jaya is proposed. MRL-Jaya is a hybridization of Jaya algorithms with modified random localization basedDE(MRLDE) algorithm MRL-Jaya connects two algorithms by a systematic approach to utilize the advantage of both in a single variant. The importance of planned algorithm is discussed later in the paper. Organization of the paper as follow; Introduction of MRLDE and Jaya Algorithm is given in section 2. Proposed MRL-Jaya is explained in section-3. In section-4, explanation of Benchmark functions, various parameter settings, performance criteria, results and comparison of MRL-Jaya with other variants are discussed. In last the entire study has concluded in section 5:

# 2 Related Work

In this section basic structure and working of Jaya and MRLDE is explained as follows:

# **2.1 MRLDE:**

MRLDE is an enhanced DE variant which is developed by taking base vector in an organized way to do mutation operation. This algorithm starts by a uniform distributed and randomly generated population of size N, say  $POP = \{P_i(g) : i = 1 : N\}$ . Now the search space is divided in three sub-regions say  $POP_{best}(g)$ ,  $POP_{medium}(g)$ , and  $POP_{worst}(g)$  according to fitness value of vectors After that mutation, crossover and selection operation are performed as defined in MRLDE algorithm as below;

i **Mutation:** Select three mutually different vectors  $P_{b1}(g)$ ,  $P_{b2}(g)$  and  $P_{b3}(g)$  from subregions  $OP_{best}(g)$ ,  $POP_{medium}(g)$  and  $POP_{worst}(g)$  respectively for any target vector  $P_i(g)$ and produce mutant vector by equation-1;

$$Y_i(g) = P_{b1}(g) + SC * [P_{b2}(g) - P_{b2}(g)]$$
(2.1)

Here SC is control factor contain value between [0, 2].

ii **Crossover:** By this operation, a trial vector  $T_i(g) = \{t_{1,i}, t_{2,i}, ..., t_{D,i}\}$  for  $P_i(g)$  is generated by equation-2;

$$t_{j,i}(g) = \begin{cases} y_{j,i}, \text{ if } rand_1(0, 1) < CR \mid | j == k : k \in [1, 2, ..., D) \\ p_{j,i}, \text{ otherwise} \end{cases}$$
(2.2)

Here CR is crossover rate and  $rand_1(0, 1)$  is any uniform random numbers between 0 and 1.

iii Selection: Finally the supreme vector among  $P_i(g)$  and  $T_i(g)$  is selected for the next generation by equation -3;

$$P_i(g+1) = \begin{cases} T_i(g), \ if \ fun \ [T_i(g)] < fun \ [P_i(g)] \\ P_i(g), \ otherwise \end{cases}$$
(2.3)

A detailed explanation of MRLDE and its working can be found in [25] - [29].

### 2.2 Jaya Algorithm:

Like MRLDE, Jaya algorithm also starts with a uniform distributed and randomly generated population of size N, say  $POP = \{P_i(g) : i = 1 : N\}$  and then move towards the optimum solution by in the search space. Let  $P_{best}(g)$  and  $P_{worst}(g)$  are the global best and global worst vector in the search space in any generation g, then the new position for any vector  $P_i(g)$  for next generation is created by equation-4 as below:

$$P_i(g+1) = P_i(g) + rand_2[0,1] * (P_{best}(g) - |P_i(g)|) - rand_3[0,1] * (P_{worst}(g) - |P_i(g)|) (2.4)$$

where  $rand_2[0, 1]$  and  $rand_3[0, 1]$  are any uniform random numbers between 0 and 1. Now old vector  $P_i(g)$  is replaced by new generated vector  $P_i(g+1)$  if it has greater fitness value than  $P_i(g+1)$  otherwise  $P_i(g)$  will be retained for the next generation as given in equation -5.

$$P_i(g+1) = \begin{cases} P_i(g+1), \ if \ fun\{P_i(g+1)\} < fun\{P_i(g)\} \\ P_i(g) \ else \end{cases}$$
(2.5)

The process will be repeated for each vector and generated a new population for next generation.



#### Working of MRL-Jaya

# 3 Proposed MRL-Jaya:

MRLDE and Jaya are both prominent algorithms for global optimization. However they both do not gives assurance to grant optimum solution for all time. It has been checked that Jaya algorithm perform with a slow convergence rate however MRLDE having fast convergence but can be stuck in local optima due to its greedy nature. MRL-Jaya is a simple and systematic hybridization of Jaya and MRLDE which overcome the disadvantages of both algorithms. First it starts with MRLDE algorithm and produced a trial vector  $T_i(g)$  corresponding to target vector  $P_i(g)$  as defined in section 2. Now if it is rejected for next generation then a new vector  $P_i(g+1)$ being created by Jaya algorithm with respect to same  $P_i(g)$  and applied the selection procedure based on fitness value as defined for Jaya algorithm is section 2 by equation-5. By doing this we have an additional choice to find a new better vector corresponding to  $P_i(g)$  and consequently we can improve the solution quality in each generation.

# 4 Result and Discussion

Various experiments have been conducted to check the significance of the proposed *MRL*-Jaya algorithm. A detail explanation of benchmark functions, parameter settings, comparison criteria and statistical result analysis is discussed in this section.

# 4.1 Benchmark Problems:

The experiments have been carried out on 13 non-shifted traditional and 6 shifted benchmark functions. All benchmark problems have been taken from various literatures [5],[6],[41] given and given in Table-1 with their important properties.

#### 4.2 Performance Measures:

The performance of algorithms has checked by following performance measures:

| F      | Name   | Property   | Boundary            | Global value |
|--------|--|--|---------------------|--------------|
| F1     | Sphere Function                                    | Unimodal, Seperable, Scalable  | $[-100, 100]^{-D}$  | 0            |
| F2     | Schwefel's Problem 2.22                            | Unimodal, Seperable, Scalable  | $[-10, 10]^{D}$     | 0            |
| F3     | Schwefel's Problem 1.2                             | Unimodal, Non-seperable, Scalable  | $[-100, 100]^{D}$   | 0            |
| F4     | Schwefel's Problem 2.21                            | Unimodal, Non-seperable, Scalable  | $[-100, 100]^{D}$   | 0            |
| F5     | Generalized Rosenbrock's Function                  | Multimodal, Non-seperable, Scalable, narrow velly from local to global optimum         | $[-30, 30]^{D}$     | 0            |
| F6     | Step Function                                      | Unimodal, Seperable, Scalable  | $[-100, 100]^p$     | 0            |
| F7     | Noise Function                                     | Unimodal, Seperable, Scalable  | $[-1.28, 1.28]^D$   | 0            |
| F8     | Quartic Noise Function                             | Multimodal, Seperable, Scalable, many local minima                                     | $[-500, 500]^{D}$   | 0            |
| F9     | Generalized Rastrigin's Function                   | Multimodal, Seperable, Scalable, many local minima                                     | $[-5.12, 5.12]^D$   | 0            |
| F10    | Multimodal, Seperable, Scalable, Ackley's Function | $[-32, 32]^D$  | 0                   |              |
| F11    | Generalized Griewank Function                      | Multimodal, Seperable, Scalable, many local minima                                     | $[-600, 600]^{D}$   | 0            |
| F12    | Generalized Penalized Functions-I                  | Multimodal, Seperable, Scalable, many local  |                     |              |
| F13    | Generalized Penalized Functions-II                 | Multimodal, Seperable, Scalable, many local minima                                     | $[-50, 50]^{D}$     | 0            |
| $SF_I$ | Shifted Sphere Function                            | Shifted, Unimodal, Seperable, Scalable   | $[-100, 100]^{D}$   | -450         |
| $SF_2$ | Shifted Schwefel 2.21 Function                     | Shifted, Unimodal, Non-seperable, Scalable   | $[-100, 100]^{D}$   | -450         |
| $SF_3$ | Shifted Rosenbrock Function                        | Shifted, Multimodal, Nonseperable, Scalable, Nerrow velly from local to global optimum | $[-100, 100]^{D}$   | 390          |
| $SF_4$ | Shifted Retrigin Function                          | Shifted, Multimodal, Seperable, Scalable, Several local optimum                        | $[-5.12, 5.12]^{D}$ | -330         |
| $SF_5$ | Shifted Griewank Function                          | Shifted, Multimodal, Nonseperable, Scalable  | $[-600, 600]^{D}$   | -180         |
| $SF_6$ | Shifted Ackley Function                            | Shifted, Multimodal, Seperable, Scalable,  | $[-32, 32]^{D}$     | -140         |

Table 1. Benchmark Functions

| Table 2. | Parameter | Settings |
|----------|-----------|----------|
|----------|-----------|----------|

| S.No | Parameter Name                                   | Parameter Setting             |
|------|--|-------------------------------|
| 1    | Population Size (N)                              | 100                           |
| 2    | Dimension (D)                                    | 30                            |
| 3    | Scale Factor $Sc$ for MRLDE and MRL-Jaya         | 0.5                           |
| 4    | Crossover Factor Cr for MRLDE and MRL-Jaya       | 0.9                           |
| 5    | Size of $N_1,\ N_2,\ N_3$ for MRLDE and MRL-Jaya | 20%, 40% and 40% respectively |
| 6    | Total Run  | 100                           |
| 7    | Software Used                                    | Matlab, Dev C++, Sigma Plot,  |

- i Average Error: The minimum error x|f(X) f(X\*)| where X\* is the global optimum, is verified when the fixed Max iteration is attained in each run. After that the average error and standard deviation is taken of all run.
- ii Average NFEs: The number of function evaluations (NFEs) is calculated when fixed error (VTR) is achieved i.e counted total NFE for  $|f(X) f(X^*)| \le VTR$  in each run.
- iii Acceleration Rate:  $AR = (1 \frac{NFE_A}{NFE_B})$
- iv **Convergence graphs:** The convergence graphs show the average fitness presentation in an experiment.

#### 4.3 Parameter Setting:

Parameter settings for the study are given in Table-2. All parameter settings have been taken same to all so that a fair comparison and analysis can be carried out. All experiments are executed on a laptop with 8*GB* memory, 2.6*GHZCPU*, intel core<sup>TM</sup> i3 processor, 64-bit, Windows 10 and using software like Matlab *R*2012b and DEVC + +.

### 4.4 Results and Comparison of MRL-Jaya with Jaya and MRLDE Algorithm:

In this section comparison of MRL-Jaya with its parent algorithm Jaya and MRLDE algorithm is discussed. The numerical results have been taken in term of error by fixing the maximum iteration for all functions as shown in Table-3. Here it can be easily observed that proposed MRL-Jaya accomplished the desire results for all function compare to others. A non-parametric Wilcoxon statistical test is also performed which can be shown in last two columns of Table. We can simply see that MRL-Jaya gives better performance than all other algorithm except function F9 where Java gives superior performance among all algorithms. For function F6 and F8, all algorithms perform similar while there is no significant difference between the performance of MRLDE and MRL-Jaya performs for the F7 and F11.

| Fun | Max-Iteration | Mean Error (Standard Deviation) |           |           |     | Wilcoxon Test |  |  |
|-----|---------------|---------------------------------|-----------|-----------|-----|---------------|--|--|
|     |               | Jaya                            | MRLDE     | MRL-Jaya  | 3/1 | 3/2           |  |  |
| F1  | 1500          | 2.06E-16                        | 1.37E-42  | 1.33E-47  | +   | +             |  |  |
|     | 1300          | -7.87E-16                       | -1.56E-42 | -6.81E-47 |     |               |  |  |
| F2  | 1500          | 5.23E-08                        | 4.66E-21  | 7.48E-23  | +   | +             |  |  |
|     | 1500          | -5.37E-08                       | -3.20E-21 | -2.15E-23 |     |               |  |  |
| F3  | 2000          | 2.86E-05                        | 1.72E-21  | 1.11E-22  | +   | +             |  |  |
|     | 3000          | -1.44E-05                       | -1.03E-21 | -2.36E-22 |     |               |  |  |
| F4  | 2000          | 5.74E-05                        | 1.96E-15  | 7.71E-22  | +   | +             |  |  |
|     | 3000          | -1.11E-05                       | -1.37E-15 | -7.37E-22 |     |               |  |  |
| F5  | 2000          | 6.05E+00                        | 8.90E-18  | 2.71E-23  | +   | +             |  |  |
|     | 2000          | -1.16E-01                       | -3.87E-18 | -2.36E-23 |     |               |  |  |
| F6  | 1500          | 0.00E+00                        | 0.00E+00  | 0.00E+00  | =   | =             |  |  |
|     | 1500          | 0.00E+00                        | 0.00E+00  | 0.00E+00  |     |               |  |  |
| F7  | 2000          | 5.51E-03                        | 2.03E-03  | 1.50E-03  | +   | =             |  |  |
|     | 3000          | -4.91E-03                       | -7.45E-05 | -9.93E-05 |     |               |  |  |
| F8  | 2000          | 1.01E-03                        | 1.01E-03  | 1.01E-03  | =   | =             |  |  |
|     | 3000          | -8.21E-03                       | -2.40E-03 | -1.42E-03 |     |               |  |  |
| F9  | 2000          | 8.20E-17                        | 9.01E-01  | 3.10E-07  | -   | +             |  |  |
|     | 3000          | -2.31E-17                       | -2.30E-01 | -5.60E-07 |     |               |  |  |
| F10 | 1500          | 4.67E-09                        | 3.40E-15  | 4.15E-16  | +   | +             |  |  |
|     | 1500          | -4.77E-09                       | 0.00E+00  | 0.00E+00  |     |               |  |  |
| F11 | 1000          | 5.96E-09                        | 0.00E+00  | 0.00E+00  | +   | =             |  |  |
|     | 1000          | -2.07E-09                       | 0.00E+00  | 0.00E+00  |     |               |  |  |
| F12 | 1000          | 1.02E-10                        | 1.35E-19  | 0.00E+00  | +   | +             |  |  |
|     | 1000          | -6.69E-10                       | 0.00E+00  | 0.00E+00  |     |               |  |  |
| F13 | 1000          | 1.19E-09                        | 1.29E-19  | 0.00E+00  | +   | +             |  |  |
|     | 1000          | -9.96E-10                       | 0.00E+00  | 0.00E+00  |     |               |  |  |
| SF1 | 500           | 3.08E-02                        | 5.68E-11  | 1.70E-13  | +   | +             |  |  |
|     | 500           | -3.56E-02                       | -1.21E-11 | -2.32E-13 |     |               |  |  |
| SF2 | 1500          | 4.22E-01                        | 4.45E-07  | 9.76E-08  | +   | +             |  |  |
|     | 1500          | -1.06E-01                       | -8.27E-07 | -8.78E-08 |     |               |  |  |
| SF3 | 1.500         | 1.23E+00                        | 4.34E-06  | 1.81E-11  | +   | +             |  |  |
|     | 1500          | -3.21E+00                       | -6.64E-06 | -6.34E-11 |     |               |  |  |
| SF4 | 1500          | 3.73E+02                        | 1.38E+02  | 1.85E+01  | +   | +             |  |  |
|     | 1500          | -3.12E+01                       | -2.80E+01 | -4.45E+00 |     |               |  |  |
| SF5 | 500           | 5.33E-03                        | 1.17E-09  | 1.70E-13  | +   | +             |  |  |
|     | 500           | (6.28E-03                       | -1.45E-09 | -1.67E-14 |     |               |  |  |
| SF6 | 500           | 4.04E-02                        | 2.85E-06  | 2.85E-08  | +   | +             |  |  |
|     | 500           | (2.17E-02                       | -2.24E-06 | -2.24E-08 |     |               |  |  |

**Table 3.** Results and Comparisons in term of Mean Error, standard deviation and Wilcoxon test at a = 0.05. Here '1', '2', '3' denote 'Jaya', 'MRLDE' and 'MRL-Jaya' respectively

'+', '=' and '-' indicate best, equal and worst performance respectively.

|     |                   |          | 1      |            | 0                |                   |  |
|-----|-------------------|----------|--------|------------|------------------|-------------------|--|
| Fun | VTR               | Mean NFE |        |            | AR               |                   |  |
|     |                   | Jaya     | MRLDE  | MRLJaya    | MRL-Jaya vs/Jaya | MRL-Jaya vs/MRLDE |  |
| F1  | $10^{-08}$        | 982100   | 42000  | 38300      | 96.10            | 8.81              |  |
| F2  | $10^{-08}$        | 182000   | 68000  | 64800      | 64.40            | 4.71              |  |
| F3  | 10 <sup>-05</sup> | 265000   | 118000 | 104000     | 60.75            | 11.86             |  |
| F4  | $10^{-05}$        | 188000   | 114000 | 94000      | 50.00            | 17.54             |  |
| F5  | 10 <sup>-08</sup> | NA       | 148000 | 127100     | NA               | 14.12             |  |
| F6  | $10^{-08}$        | 22000    | 14000  | 12400      | 43.64            | 11.43             |  |
| F7  | $10^{-02}$        | 152000   | 68000  | 46500      | 69.41            | 31.62             |  |
| F8  | $10^{-03}$        | 106000   | 112000 | 96000      | 9.43             | 14.29             |  |
| F9  | 10 <sup>-08</sup> | 264000   | NA     | 322000     | -21.97           | NA                |  |
| F10 | 10 <sup>-08</sup> | 144000   | 62000  | 59900      | 58.40            | 3.39              |  |
| F11 | $10^{-08}$        | 100000   | 44000  | 40900      | 59.10            | 7.05              |  |
| F12 | $10^{-08}$        | 84500    | 36000  | 34700      | 58.93            | 3.61              |  |
| F13 | $10^{-08}$        | 96000    | 41000  | 36700      | 61.77            | 10.49             |  |
| SF1 | $10^{-08}$        | 81000    | 43000  | 38000      | 53.09            | 11.63             |  |
| SF2 | 10 <sup>-06</sup> | NA       | 122000 | 105000     | NA               | 13.93             |  |
| SF3 | 10 <sup>-06</sup> | NA       | 140000 | 135000     | NA               | 3.57              |  |
| SF4 | $10^{-08}$        | NA       | NA     | NA         | NA               | Na                |  |
| SF5 | $10^{-08}$        | 83000    | 47000  | 38000      | 54.22            | 19.15             |  |
| SF6 | $10^{-06}$        | 128000   | 65000  | 55000      | 57.03            | 15.38             |  |
|     |                   |          |        | Average AR | 51.62            | 11.92             |  |

 Table 4. Results and Comparisons in term of average NFE and Acceleration Rate

Table-4 demonstrates the numerical results in term of average NFE and acceleration rate (AR) of 100 runs. Here it can be observed that proposed MRL-Jaya takes fewer NFE to attain the set error for each function except for function F9 except F9 where Jaya takes less NFE than all others. All algorithms are unable to reach the fixed error in case of function SF4. By acceleration rate (AR), we can also verify the fast convergence speed of proposed algorithm compare to both Jaya and MRLDE for each function (except F9 and SF4). It is also observed that MRL-Jaya improves the average convergence speed by 51.62% and 11.92% compare to Jaya and MRLDE respectively.

# 4.5 Results and Comparison of MRL-Jaya with DE, ODE jDE, LeDE:

In this section comparison of proposed MRL-Jaya with DE and its other modified variants ODE [2], jDE [3] and LeDE [6] has been carried out. The numerical results have taken in term of average-NFE of 100 runs by fixing error as 10-08 for all function except function F7 for which error is taken as 10 - 02. Parameter settings and numerical results for ODE, jDE and LeDE are taken from [6]. From the Table-5, it can be easily observed that proposed MRL-Jaya attain desire results rapidly compare to all other algorithm for all function except F3, F8 and F9. LeDE gives best performance for F3 while jDE gives perform superior for F8 and F9. The rank-wise performance of all algorithms is also given in Table-5 for each function. The average rank of LeDE, jDE, ODE and DE are 1.92, 2.92, 3.85 and 4.77 whereas the average rank of MRL-Jaya is 1.54 which proved the superiority and robustness in performance of proposed MRL-Jaya on others.

| En  | Average NFE |         |        |          |          | Rank |      |     |      |           |
|-----|-------------|---------|--------|----------|----------|------|------|-----|------|-----------|
| n   | DE          | ODE     | jDE    | LeDE     | MRL-Jaya | DE   | OD E | jDE | LeDE | MRL -Jaya |
| F1  | 104000      | 67,524  | 60000  | 49,494   | 38300    | 5    | 4    | 3   | 2    | 1         |
| F2  | 174000      | 140,170 | 83000  | 77,464   | 64800    | 5    | 4    | 3   | 2    | 1         |
| F3  | 422000      | 489,210 | 340000 | 140, 176 | 146000   | 4    | 5    | 3   | 1    | 2         |
| F4  | NA          | 145,880 | 300000 | 157,499  | 132100   | 5    | 3    | 4   | 2    | 1         |
| F5  | 424000      | NA      | 580000 | 282,972  | 127100   | 3    | 5    | 4   | 2    | 1         |
| F6  | 36000       | 25,008  | 23000  | 17,123   | 12400    | 5    | 4    | 3   | 2    | 1         |
| F7  | 90500       | 60,230  | 100000 | 33,302   | 46500    | 5    | 3    | 4   | 2    | 1         |
| F8  | NA          | 147,472 | 89000  | 111,013  | 488000   | 5    | 3    | 1   | 2    | 4         |
| F9  | NA          | 190,604 | 120000 | 187,813  | 322000   | 5    | 3    | 1   | 2    | 4         |
| F10 | 165000      | 10,6694 | 91000  | 76,111   | 59900    | 5    | 4    | 3   | 2    | 1         |
| F11 | 112000      | 79,888  | 63000  | 50,579   | 40900    | 5    | 4    | 3   | 2    | 1         |
| F12 | 96000       | 63,710  | 55000  | 41,384   | 34700    | 5    | 4    | 3   | 2    | 1         |
| F13 | 106000      | 63,202  | 60000  | 46,529   | 36700    | 5    | 4    | 3   | 2    | 1         |

Table 5. Comparison of MRL-Jaya with DE, ODE, LeDE and SaDE in term of average NFE

#### 4.6 Convergence Graph:

In this section, the convergence graphs of Jaya, MRLDE and proposed MRL-Jaya is presented for function *F*1, *F*4, *F*5 and *F*10. The convergence speed of MRL-Jaya can be easily analyzed by these graphs over Jaya and MRLDE.

# 5 Conclusion:

In this paper, a new algorithm 'MRJ-Jaya' by fusion of MRLDE and Jaya algorithm is proposed for solving global optimization problems. The combination of two algorithms is taken in a systematic way so that the advantage of both algorithms can be utilized to improve the search ability with a high convergence speed. The proposed MRL-Jaya has been compared with its parent algorithms i.e Jaya and MRLDE in term of average error and average NFE on 13 non-shifted and 6 shifted unconstrained benchmark functions. A non-parametric Wilcoxon statistical test is also performed to analyze the comparison. Furthermore MRL-Jaya is also compared with DE and other DE variants: ODE, jDE and LeDE on 13 traditional unconstrained benchmark functions in term of average NFE and acceleration rate. The results and comparisons have revealed that the MRL-Jaya perform superior compared to other algorithms in terms of search process efficiency, solution quality and the convergence speed.

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