# ON ALMOST $\gamma$ -CONTINUOUS FUNCTIONS IN *N*-NEUTROSOPHIC CRISP TOPOLOGICAL SPACES

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Abstract In this paper, we extend a class of  $\gamma$ -continuous functions in N-neutrosophic crisp topological spaces into a new class of almost  $\gamma$ -continuous functions in N-neutrosophic crisp topological spaces. In a N-neutrosophic crisp  $\gamma$ -open set, an almost  $\gamma$ -continuous functions is a stronger forms of mapping has equally distributed to their elements in a  $\gamma$ -open set. Also, we investigate and discuss some possible outcomes in almost  $\gamma$ -continuous functions based on N-neutrosophic crisp topological spaces. In addition, an almost  $\gamma$ -continuous functions is related to other open sets such as semi-open, pre-open and  $\beta$ -open sets can bring out a results in N-neutrosophic crisp topological spaces.

## 1 Introduction

Crisp sets are utilized in our daily routine for the most of our careers. The concepts of neutrosophy and neutrosophic set are the recent tools in a topological space. It was first introduced by Smarandache [11, 12] in the beginning of  $20^{th}$  century. In 2014, Salama, Smarandache and Kroumov [8] has given the essential idea of neutrosophic crisp set in a topological space. After that Al-Omeri [2] likewise explored some essential properties of neutrosophic crisp topological Spaces. Al-Hamido [1] investigate the chance of extending the idea of neutrosophic crisp topological spaces into N-topology and research a portion of their essential properties in N-terms. By utilizing N-terms, we can characterized as  $1_{nc}ts, 2_{nc}ts, \dots, N_{nc}ts$ .

In 1996, Andrijevic [4] introduced *b*-open sets and develop some of their works in general topology. Ogata [7] characterized an activity  $\gamma$  on a topological space and presented  $\gamma$ -open sets. Additionally, the thought of  $\gamma$ -open set in topological spaces was first presented by Min [6] and worked in the field of general topology. Basu et al. [5] presented a kind of continuity called  $\gamma$ -continuous function. Vadivel [15] presented  $\gamma$ -open sets in neutrosophic crisp topological spaces via *N*-terms of topology. Also  $\gamma$ -continuous function in a *N*-neutrosophic crisp topological spaces was introduced by Singal and Singal [10]. Recently, many authors [3, 13, 19, 20] worked on almost properties of continuous functions in neutrosophic set, neutrosophic crisp set, neutrosophic multifunctions, etc.

Research gap: The extension  $\gamma$ -continuous function in a neutrosophic topological spaces can never be studied before and also in a neutrosophic crisp topological spaces. An almost concept of mappings can be defined by very few due to the stronger content of the set. The concept of *N*neutrosophic crisp almost  $\gamma$ -continuous functions in a *N*-neutrosophic crisp topological spaces cannot be examined before and study in this paper with some of their properties.

In this paper, we discuss a new class of functions called N-neutrosophic crisp almost  $\gamma$ continuous functions in a N-neutrosophic crisp topological spaces. Also, we study and research about N-neutrosophic crisp almost  $\gamma$ -continuous functions and study some of their properties. Finally, we discuss N-neutrosophic crisp almost  $\gamma$ -continuous functions related to some other open sets in N-neutrosophic crisp topological spaces.

## 2 Preliminaries

Some basic definitions & properties of  $N_{nc}$  topological spaces are discussed in this section.

**Definition 2.1.** [9] For any non-empty fixed set Y, a neutrosophic crisp set (briefly, ncs) L, is an object having the form  $L = \langle L_1, L_2, L_3 \rangle$  where  $L_1, L_2$  and  $L_3$  are subsets of Y satisfying any one of the types

(T1) 
$$L_{\iota} \cap L_{\kappa} = \phi, \iota \neq \kappa \& \bigcup_{\iota=1}^{3} L_{\iota} \subset Y, \forall \iota, \kappa = 1, 2, 3.$$
  
(T2)  $L_{\iota} \cap L_{\kappa} = \phi, \iota \neq \kappa \& \bigcup_{\iota=1}^{3} L_{\iota} = Y, \forall \iota, \kappa = 1, 2, 3.$   
(T3)  $\bigcap_{\iota=1}^{3} L_{\iota} = \phi \& \bigcup_{\iota=1}^{3} L_{\iota} = Y, \forall \iota = 1, 2, 3.$ 

**Definition 2.2.** [9] Types of ncs's  $\emptyset_N$  and  $Y_N$  in Y are as

- (i)  $\emptyset_N$  may be defined as  $\emptyset_N = \langle \emptyset, \emptyset, Y \rangle$  or  $\langle \emptyset, Y, Y \rangle$  or  $\langle \emptyset, Y, \emptyset \rangle$  or  $\langle \emptyset, \emptyset, \emptyset \rangle$ .
- (ii)  $Y_N$  may be defined as  $Y_N = \langle Y, \emptyset, \emptyset \rangle$  or  $\langle Y, Y, \emptyset \rangle$  or  $\langle Y, \emptyset, Y \rangle$  or  $\langle Y, Y, Y \rangle$ .

**Definition 2.3.** [9] Let Y be a non-empty set & the ncs's L & M in the form  $L = \langle L_1, L_2, L_3 \rangle$ ,  $M = \langle M_1, M_2, M_3 \rangle$ , then

- (i)  $L \subseteq M \Leftrightarrow L_1 \subseteq M_1, L_2 \subseteq M_2 \& L_3 \supseteq M_3 \text{ or } L_1 \subseteq M_1, L_2 \supseteq M_2 \& L_3 \supseteq M_3.$
- (ii)  $L \cap M = \langle L_1 \cap M_1, L_2 \cap M_2, L_3 \cup M_3 \rangle$  or  $\langle L_1 \cap M_1, L_2 \cup M_2, L_3 \cup M_3 \rangle$
- (iii)  $L \cup M = \langle L_1 \cup M_1, L_2 \cup M_2, L_3 \cap M_3 \rangle$  or  $\langle L_1 \cup M_1, L_2 \cap M_2, L_3 \cap M_3 \rangle$

**Definition 2.4.** [9] Let  $L = \langle L_1, L_2, L_3 \rangle$  a *ncs* on *Y*, then the complement of *L* (briefly,  $L^c$ ) may be defined in three different ways:

- (C1)  $L^{c} = \langle L_{1}^{c}, L_{2}^{c}, L_{3}^{c} \rangle$ , or (C2)  $L^{c} = \langle L_{3}, L_{2}, L_{1} \rangle$ , or

(C3)  $L^c = \langle L_3, L_2^c, L_1 \rangle.$ 

**Definition 2.5.** [8] A neutrosophic crisp topology (briefly, nct) on a non-empty set Y is a family  $\Gamma$  of nc subsets of Y satisfying

- (i)  $\emptyset_N, Y_N \in \Gamma$ .
- (ii)  $L_1 \cap L_2 \in \Gamma \forall L_1 \& L_2 \in \Gamma$ .
- (iii)  $\bigcup L_{\iota} \in \Gamma, \forall L_{\iota} : \iota \in T \subseteq \Gamma.$

Then  $(Y, \Gamma)$  is a neutrosophic crisp topological space (briefly, *ncts* for short) in Y. The neutrosophic crisp open sets (briefly, *ncos*) are the elements of  $\Gamma$  in Y. A *ncs* C is closed (briefly, *nccs*) iff its complement  $C^c$  is *ncos*.

**Definition 2.6.** [1] Let Y be a non-empty set. Then  ${}_{nc}\Gamma_1, {}_{nc}\Gamma_2, \cdots, {}_{nc}\Gamma_N$  are N-arbitrary crisp topologies defined on Y and the collection

$$N_{nc}\Gamma = \{G \subseteq Y : G = (\bigcup_{\iota=1}^{N} G_{\iota}) \cup (\bigcap_{\iota=1}^{N} H_{\iota}), G_{\iota}, H_{\iota} \in {}_{nc}\Gamma_{\iota}\}$$

is called  $N_{nc}$ -topology on Y if the axioms are satisfied:

- (i)  $\emptyset_N, Y_N \in N_{nc}\Gamma$ .
- (ii)  $\bigcup_{\iota=1}^{\infty} C_{\iota} \in N_{nc} \Gamma \forall \{C_{\iota}\}_{\iota=1}^{\infty} \in N_{nc} \Gamma.$
- (iii)  $\bigcap_{\iota=1}^{n} C_{\iota} \in N_{nc} \Gamma \forall \{C_{\iota}\}_{\iota=1}^{n} \in N_{nc} \Gamma.$

Then  $(Y, N_{nc}\Gamma)$  is called a  $N_{nc}$ -topological space (briefly,  $N_{nc}ts$ ) on Y. The  $N_{nc}$ -open sets  $(N_{nc}os)$  are the elements of  $N_{nc}\Gamma$  in Y and the complement of  $N_{nc}os$  is called  $N_{nc}$ -closed sets  $(N_{nc}cs)$  in Y. The elements of Y are known as  $N_{nc}$ -sets  $(N_{nc}s)$  on Y.

**Definition 2.7.** [1] Let  $(Y, N_{nc}\Gamma)$  be  $N_{nc}ts$  on Y and L be an  $N_{nc}s$  on Y, then the  $N_{nc}$  interior of L (briefly,  $N_{nc}int(L)$ ),  $N_{nc}$  closure of L (briefly,  $N_{nc}cl(L)$ ) are defined as

$$N_{nc}int(L) = \bigcup \{ C : C \subseteq L \& C \text{ is a } N_{nc}os \text{ in } Y \}$$

$$N_{nc}cl(L) = \cap \{A : L \subseteq A \& A \text{ is a } N_{nc}cs \text{ in } Y\}.$$

**Definition 2.8.** [1] Let  $(Y, N_{nc}\Gamma)$  be any  $N_{nc}ts$ . Let L be an  $N_{nc}s$  in  $(Y, N_{nc}\Gamma)$ . Then L is said to be a  $N_{nc}$ -regular (resp.  $N_{nc}$ -pre,  $N_{nc}$ -semi,  $N_{nc}-\alpha$ ,  $N_{nc}-\gamma$  &  $N_{nc}-\beta$ ) open set (briefly,  $N_{nc}ros$  [15] (resp.  $N_{nc}\mathcal{P}os$ ,  $N_{nc}\mathcal{S}os$ ,  $N_{nc}\alpha os$ ,  $N_{nc}\gamma os$  [15] &  $N_{nc}\beta os$  [17])) if  $L = N_{nc}int(N_{nc}cl(L))$  (resp.  $L \subseteq N_{nc}int(N_{nc}cl(L))$ ,  $L \subseteq N_{nc}cl(N_{nc}int(L))$ ,  $L \subseteq N_{nc}cl(N_{nc}int(N_{nc}cl(L)))$ ,  $L \subseteq N_{nc}cl(N_{nc}int(N_{nc}cl(L)))$ .

The complement of an  $N_{nc}\mathcal{P}os$  (resp.  $N_{nc}\mathcal{S}os$ ,  $N_{nc}\alpha os$ ,  $N_{nc}ros$ ,  $N_{nc}\gamma os$  &  $N_{nc}\beta os$ ) is called an  $N_{nc}$ -pre (resp.  $N_{nc}$ -semi,  $N_{nc}-\alpha$ ,  $N_{nc}$ -regular,  $N_{nc}-\gamma$  &  $N_{nc}-\beta$ ) closed set (briefly,  $N_{nc}\mathcal{P}cs$  (resp.  $N_{nc}\mathcal{S}cs$ ,  $N_{nc}\alpha cs$ ,  $N_{nc}rcs$ ,  $N_{nc}\gamma cs$  &  $N_{nc}\beta cs$ )) in Y.

The family of all  $N_{nc}\mathcal{P}os$  (resp.  $N_{nc}\mathcal{P}cs$ ,  $N_{nc}\mathcal{S}os$ ,  $N_{nc}\mathcal{S}cs$ ,  $N_{nc}\alpha os$ ,  $N_{nc}\alpha cs$ ,  $N_{nc}\gamma os$ ,  $N_{nc}\gamma cs$ ,  $N_{nc}\beta os$ , &  $N_{nc}\beta cs$ ) of Y is denoted by  $N_{nc}\mathcal{P}OS(Y)$  (resp.  $N_{nc}\mathcal{P}CS(Y)$ ,  $N_{nc}\mathcal{S}OS(Y)$ ,  $N_{nc}\mathcal{S}OS(Y)$ ,  $N_{nc}\alpha OS(Y)$ ,  $N_{nc}\alpha CS(Y)$ ,  $N_{nc}\gamma OS(Y)$ ,  $N_{nc}\gamma CS(Y)$ ,  $N_{nc}\beta OS(Y)$  &  $N_{nc}\beta CS(Y)$ ).

**Definition 2.9.** [14] Let  $(Y, N_{nc}\Gamma)$  &  $(Z, N_{nc}\Psi)$  be any two  $N_{nc}ts$ 's. A map  $h : (Y, N_{nc}\Gamma) \rightarrow (Z, N_{nc}\Psi)$  is said to be  $N_{nc}$ -continuous (briefly,  $N_{nc}Cts$ ) if the inverse image of every  $N_{nc}os$  in  $(Z, N_{nc}\Psi)$  is a  $N_{nc}os$  in  $(Y, N_{nc}\Gamma)$ .

**Definition 2.10.** [18] Let  $(Y, N_{nc}\Gamma)$  be  $N_{nc}ts$  on Y and L be an  $N_{nc}s$  on Y, then the  $N_{nc}\delta$  interior of L (briefly,  $N_{nc}\delta int(L)$ ) and  $N_{nc}\delta$  closure of L (briefly,  $N_{nc}\delta cl(L)$ ) are defined as

$$N_{nc}\delta int(L) = \bigcup \{A : A \subseteq L \& A \text{ is a } N_{nc}ros\}$$

$$\begin{split} N_{nc}\delta cl(L) &= \cup \{y \in Y : N_{nc}int(N_{nc}cl(L)) \cap L \neq \phi, \ y \in L \ \& \ L \ \text{is a} \ N_{nc}os\} \ \text{or} \\ &N_{nc}\delta cl(L) = \cap \{A : L \subseteq A \ \& \ A \ \text{is a} \ N_{nc}rcs \ \text{in} \ Y\}. \end{split}$$

**Definition 2.11.** [18] Let  $(Y, N_{nc}\Gamma)$  be any  $N_{nc}ts$ . Let L be an  $N_{nc}s$  in  $(Y, N_{nc}\Gamma)$ . Then L is said to be a  $N_{nc}\delta$  open set (briefly,  $N_{nc}\delta os$ ) if  $L = N_{nc}\delta int(L)$ .

The complement of an  $N_{nc}\delta os$  is called an  $N_{nc}$ - $\delta$  closed set (briefly,  $N_{nc}\delta cs$ ) in Y.

### **3** $N_{nc}$ Almost $\gamma$ -Continuous Function

Here we study about  $N_{nc}$  almost  $\gamma$ -continuous function and its properties in  $N_{nc}ts$ .

**Definition 3.1.** [16] Let  $(Y, N_{nc}\Gamma)$  &  $(Z, N_{nc}\Psi)$  be any two  $N_{nc}ts$ 's. A map  $h : (Y, N_{nc}\Gamma) \rightarrow (Z, N_{nc}\Psi)$  is said to be  $N_{nc}\gamma$ -continuous (briefly,  $N_{nc}\gamma Cts$ ) if the inverse image of every  $N_{nc}os$  in  $(Z, N_{nc}\Psi)$  is a  $N_{nc}\gamma os$  in  $(Y, N_{nc}\Gamma)$ .

**Definition 3.2.** [16] Let  $L = \langle L_1, L_2, L_3 \rangle$  a  $N_{nc}s$  on Y, then  $p = \langle pt_1, pt_2, pt_3 \rangle$ ,  $pt_1 \neq pt_2 \neq pt_3 \in Y$  is called a N-neutrosophic crisp point (briefly,  $N_{nc}p$ ).

A  $N_{nc}p$ ,  $p = \langle pt_1, pt_2, pt_3 \rangle$  belongs to a  $N_{nc}s L = \langle L_1, L_2, L_3 \rangle$  of Y, denoted by  $p \in L$ , if it may be defined in two ways

- (i)  $\{pt_1\} \subseteq L_1, \{pt_2\} \subseteq L_2 \& \{pt_3\} \supseteq L_3$  or
- (ii)  $\{pt_1\} \subseteq L_1, \{pt_2\} \supseteq L_2 \& \{pt_3\} \supseteq L_3.$

**Definition 3.3.** A function  $h : (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$  is called *N*-neutrosophic crisp almost continuous at a  $N_{nc}p \ p \in Y$  if  $\forall N_{nc}os \ M$  in *Z* containing h(p), there exists a  $N_{nc}os \ L$  in *Y* containing  $p \ni h(L) \subseteq N_{nc}int(N_{nc}cl(M))$ . If *h* is *N*-neutrosophic crisp almost continuous at every  $N_{nc}p$  of *Y*, then it is called *N*-neutrosophic crisp almost continuous (briefly,  $N_{nc}aCts$ ).

**Definition 3.4.** A function  $h : (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$  is called *N*-neutrosophic crisp almost  $\gamma$ -continuous at a  $N_{nc}p$ ,  $p \in Y$  if  $\forall p \in Y$  and each  $N_{nc}os M$  of *Z* containing h(p), there exists a  $N_{nc}\gamma os L$  of *Y* containing  $p \ni h(L) \subseteq N_{nc}int(N_{nc}cl(M))$ . If *h* is *N*-neutrosophic crisp almost  $\gamma$ -continuous at every  $N_{nc}p$  of *Y*, then it is called *N*-neutrosophic crisp almost  $\gamma$ -continuous (briefly,  $N_{nc}a\gamma Cts$ ).

Remark 3.5. The following implications are easily shown and the converses are not true.

 $\boxed{N_{nc}\gamma Cts} \implies \boxed{N_{nc}a\gamma Cts} \implies \boxed{N_{nc}aCts}$ 

**Example 3.6.** Let  $Y = \{l, m, n\}$ ,  $_{nc}\Gamma_1 = \{\phi_N, Y_N, A, B, C\}$ ,  $_{nc}\Gamma_2 = \{\phi_N, Y_N, D\}$ .  $A = \langle \{l\}, \{\phi\}, \{m, n\} \rangle$ ,  $B = \langle \{m\}, \{\phi\}, \{l, n\} \rangle$ ,  $C = \langle \{l, m\}, \{\phi\}, \{n\} \rangle$ ,  $D = \langle \{l, n\}, \{\phi\}, \{m\} \rangle$ , then we have  $2_{nc}\Gamma = \{\phi_N, Y_N, A, B, C, D\}$ .  $_{nc}\Phi_1 = \{\phi_N, Y_N, T, U, V\}$ ,  $_{nc}\Phi_2 = \{\phi_N, Y_N, W\}$ .  $T = \langle \{l\}, \{\phi\}, \{m, n\} \rangle$ ,  $U = \langle \{m\}, \{\phi\}, \{l, n\} \rangle$ ,  $V = \langle \{l, m\}, \{\phi\}, \{n\} \rangle$ ,  $W = \langle \{l, n\}, \{\phi\}, \{m\} \rangle$ ,  $\{m\} \rangle$ , then we have  $2_{nc}\Phi = \{\phi_N, Y_N, T, U, V, W\}$ . Let  $h : (Y, 2_{nc}\Gamma) \to (Y, 2_{nc}\Phi)$  be defined as h(l) = n, h(m) = m and h(n) = l. an identity function. Then h is  $2_{nc}a\gamma Cts$  but not  $2_{nc}\gamma Cts$ , because  $\langle \{l\}, \{\phi\}, \{m, n\} \rangle$  is a  $2_{nc}os$  in  $(Y, 2_{nc}\Phi)$  containing  $h(\langle \{n\}, \{\phi\}, \{l, m\} \rangle) = \langle \{l\}, \{\phi\}, \{m, n\} \rangle$ , but there exist no  $2_{nc}\gamma os$ ,  $\langle \{n\}, \{\phi\}, \{l, m\} \rangle$  in  $(Y, 2_{nc}\Gamma)$  containing  $\langle \{n\}, \{\phi\}, \{l, m\} \rangle$ )  $\subseteq \langle \{l\}, \{\phi\}, \{m, n\} \rangle$ .

**Example 3.7.** In Example 3.6,  $h(\gamma) = Y$ , for all  $\gamma \in 2_{nc}\Gamma$ . Then h is  $2_{nc}aCts$  but not  $2_{nc}a\gamma Cts$ .

**Corollary 3.8.** Let  $(Y, N_{nc}\Gamma)$  be any  $N_{nc}$ ts. Let L be an  $N_{nc}$ s in  $(Y, N_{nc}\Gamma)$ . Then  $L \in N_{nc}\mathcal{P}OS(Y)$  if and only if  $N_{nc}\mathcal{S}cl(L) = N_{nc}int(N_{nc}cl(L))$ .

**Theorem 3.9.** For a function  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$ , then the statements

- (i) h is  $N_{nc}a\gamma Cts$ .
- (ii)  $\forall p \in Y$  and each  $N_{nc}$  os N of Z containing h(p), there exists a  $N_{nc}\gamma$  os L in Y containing  $p \ni h(L) \subseteq N_{nc} Scl(N)$ .
- (iii)  $\forall p \in Y$  and each  $N_{nc} ros N$  of Z containing h(p), there exists a  $N_{nc} \gamma os L$  in Y containing  $p \ni h(L) \subseteq N$ .
- (iv)  $\forall p \in Y$  and each  $N_{nc}\delta os N$  of Z containing h(p), there exists a  $N_{nc}\gamma os L$  in Y containing  $p \ni h(L) \subseteq N$ .

*Proof.* (i)  $\Rightarrow$  (ii) Let  $p \in Y$  and Let N be any  $N_{nc}os$  of Z containing h(p). By (i), there exists a  $N_{nc}\gamma os L$  of Y containing  $p \ni h(L) \subseteq N_{nc}int(N_{nc}cl(N))$ . Since N is  $N_{nc}os$  and hence N is  $N_{nc}\mathcal{P}os$ . By Corollary 3.1,  $N_{nc}int(N_{nc}cl(N)) = N_{nc}\mathcal{S}cl(N)$ . Therefore,  $h(L) \subseteq N_{nc}\mathcal{S}cl(N)$ .

(ii)  $\Rightarrow$  (iii) Let  $p \in Y$  and Let N be any  $N_{nc}ros$  of Z containing h(p). Then N is an  $N_{nc}os$  of Z containing h(p). By (ii), there exists a  $N_{nc}\gamma os L$  in Y containing  $p \ni h(L) \subseteq N_{nc}Scl(N)$ . Since N is  $N_{nc}ros$  and hence N is  $N_{nc}Pos$ . By Corollary 3.1,  $N_{nc}Scl(N) = N_{nc}int(N_{nc}cl(N))$ . Therefore,  $h(L) \subseteq N_{nc}int(N_{nc}cl(N))$ . Since N is  $N_{nc}ros$ , then  $h(L) \subseteq N$ .

(iii)  $\Rightarrow$  (iv) Let  $p \in Y$  and Let N be any  $N_{nc}\delta os$  of Z containing h(p). Then for each  $h(p) \in N$ , there exists a  $N_{nc}os$  G containing  $h(p) \ni G \subseteq N_{nc}int(N_{nc}cl(G)) \subseteq N$ . Since  $N_{nc}int(N_{nc}cl(G))$  is  $N_{nc}ros$  of Z containing h(p). By (iii), there exists a  $N_{nc}\gamma os$  L in Y containing  $p \ni h(L) \subseteq N_{nc}int(N_{nc}cl(G)) \subseteq N$ .

(iv)  $\Rightarrow$  (i) Let  $p \in Y$  and Let N be any  $N_{nc}os$  of Z containing h(p). Then  $N_{nc}int(N_{nc}cl(N))$ is  $N_{nc}\delta os$  of Z containing h(p). By (iv), there exists a  $N_{nc}\gamma os L$  in Y containing  $p \ni h(L) \subseteq N_{nc}int(N_{nc}cl(N))$ . Therefore, h is  $N_{nc}a\gamma Cts$ .

**Theorem 3.10.** For a function  $h : (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$ , then the statements are equivalent.

- (i) h is  $N_{nc}a\gamma Cts$ .
- (ii)  $h^{-1}(N_{nc}int(N_{nc}cl(N)))$  is  $N_{nc}\gamma$  os in Y, for each  $N_{nc}$  os N in Z.

- (iii)  $h^{-1}(N_{nc}cl(N_{nc}int(F)))$  is  $N_{nc}\gamma cs$  in Y, for each  $N_{nc}cs$  F in Z.
- (iv)  $h^{-1}(F)$  is  $N_{nc}\gamma cs$  in Y, for each  $N_{nc}rcs F$  of Z.
- (v)  $h^{-1}(N)$  is  $N_{nc}\gamma os$  in Y, for each  $N_{nc}ros N$  of Z.

*Proof.* (i)  $\Rightarrow$  (ii) Let N be any  $N_{nc}os$  in Z. We have to show that  $h^{-1}(N_{nc}int(N_{nc}cl(N)))$ is  $N_{nc}\gamma os$  in Y. Let  $p \in h^{-1}(N_{nc}int(N_{nc}cl(N)))$ . Then  $h(p) \in N_{nc}int(N_{nc}cl(N))$  and  $N_{nc}int(N_{nc}cl(N))$  is a  $N_{nc}ros$  in Z. Since h is  $N_{nc}a\gamma Cts$ . Then by Theorem 3.9, there exists a  $N_{nc}\gamma os L$  of Y containing  $p \ni h(L) \subseteq N_{nc}int(N_{nc}cl(N))$ . Which implies that  $p \in L \subseteq h^{-1}(N_{nc}int(N_{nc}cl(N)))$ . Therefore,  $h^{-1}(N_{nc}int(N_{nc}cl(N)))$  is  $N_{nc}\gamma os$  in Y.

(ii)  $\Rightarrow$  (iii) Let F be any  $N_{nc}cs$  of Z. Then  $Z \setminus F$  is an  $N_{nc}os$  of Z. By (ii),  $h^{-1}(N_{nc}int(N_{nc}cl(Z \setminus F)))$  is  $N_{nc}\gamma os$  in Y and  $h^{-1}(N_{nc}int(N_{nc}cl(Z \setminus F))) = h^{-1}(N_{nc}int(Z \setminus N_{nc}int(F))) = h^{-1}(Z \setminus N_{nc}cl(N_{nc}int(F))) = Y \setminus h^{-1}(N_{nc}cl(N_{nc}int(F)))$  is  $N_{nc}\gamma os$  in Y and hence  $h^{-1}(N_{nc}cl(N_{nc}int(F)))$  is  $N_{nc}\gamma cs$  in Y.

(iii)  $\Rightarrow$  (iv) Let F be any  $N_{nc}rcs$  of Z. Then F is a  $N_{nc}cs$  of Z. By (iii),  $h^{-1}(N_{nc}cl(N_{nc}int(F)))$  is  $N_{nc}\gamma cs$  in Y. Since F is  $N_{nc}rcs$ . Then  $h^{-1}(N_{nc}cl(N_{nc}int(F))) = h^{-1}(F)$ . Therefore,  $h^{-1}(F)$  is  $N_{nc}\gamma cs$  in Y.

(iv)  $\Rightarrow$  (v) Let N be any  $N_{nc}ros$  of Z. Then  $Z \setminus N$  is  $N_{nc}rcs$  of Z and by (iv), we have  $h^{-1}(Z \setminus N) = Y \setminus h^{-1}(N)$  is  $N_{nc}\gamma cs$  in Y and hence  $h^{-1}(N)$  is  $N_{nc}\gamma cs$  in Y.

 $(v) \Rightarrow (i)$  Let  $p \in Y$  and let N be any  $N_{nc}ros$  of Z containing h(p). Then  $p \in h^{-1}(N)$ . By (v), we have  $h^{-1}(N)$  is  $N_{nc}\gamma os$  in Y. Therefore, we obtain  $h(h^{-1}(N)) \subseteq N$ . Hence by Theorem 3.9, h is  $N_{nc}a\gamma Cts$ .

**Theorem 3.11.** For a function  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$ , then the statements are equivalent.

- (i) h is  $N_{nc}a\gamma Cts$ .
- (ii)  $h(N_{nc}\gamma cl(L)) \subseteq N_{nc}\delta cl(h(L))$ , for each subset L of Y.
- (iii)  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}\delta cl(N))$ , for each subset N of Z.
- (iv)  $h^{-1}(L)$  is  $N_{nc}\gamma cs$  in Y, for each  $N_{nc}\delta cs L$  of Z.
- (v)  $h^{-1}(N)$  is  $N_{nc}\gamma os$  in Y, for each  $N_{nc}\delta os$  N of Z.
- (vi)  $h^{-1}(N_{nc}\delta int(N)) \subseteq N_{nc}\gamma int(h^{-1}(N))$ , for each subset N of Z.
- (vii)  $N_{nc}\delta int(h(L)) \subseteq h(N_{nc}\gamma int(L))$ , for each subset L of Y.

*Proof.* (i)  $\Rightarrow$  (ii) Let *L* be a subset of *Y*. Since  $N_{nc}\delta cl(h(L))$  is  $N_{nc}\delta cs$  in *Z*. Then, we have  $L \subseteq h^{-1}(N_{nc}\delta cl(h(L)))$ . By (i) and Theorem 3.10,  $h^{-1}(N_{nc}\delta cl(h(L)))$  is  $N_{nc}\gamma cs$  of *Y*. Hence  $N_{nc}\gamma cl(L) \subseteq h^{-1}(N_{nc}\delta cl(h(L)))$ . Therefore, we obtain  $h(N_{nc}\gamma cl(L)) \subseteq N_{nc}\delta cl(h(L))$ .

(ii)  $\Rightarrow$  (iii) Let N be any subset of Z. Then  $h^{-1}(N)$  is a subset of Y. By (ii), we have  $h(N_{nc}\gamma cl(h^{-1}(N))) \subseteq N_{nc}\delta cl(h(h^{-1}(N))) = N_{nc}\delta cl(N)$ .

Hence  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}\delta cl(N)).$ 

(iii)  $\Rightarrow$  (iv) Let L be any  $N_{nc}\delta cs$  of Z. By (iii), we have  $N_{nc}\gamma cl(h^{-1}(L)) \subseteq h^{-1}(N_{nc}\delta cl(L)) = h^{-1}(L)$  and hence  $h^{-1}(L)$  is  $N_{nc}\gamma cs$  in Y.

(iv)  $\Rightarrow$  (v) Let N be any  $N_{nc}\delta os$  of Z. Then  $Z \setminus N$  is  $N_{nc}\delta cs$  of Z and by (iv), we have  $h^{-1}(Z \setminus N) = Y \setminus h^{-1}(N)$  is  $N_{nc}\gamma cs$  in Y. Hence  $h^{-1}(N)$  is  $N_{nc}\gamma os$  in Y.

 $(\mathbf{v}) \Rightarrow (\mathbf{v})$  For each subset N of Z. We have  $N_{nc}\delta int(N) \subseteq N$ . Then  $h^{-1}(N_{nc}\delta int(N)) \subseteq h^{-1}(N)$ . By  $(\mathbf{v}), h^{-1}(N_{nc}\delta int(N))$  is  $N_{nc}\gamma os$  in Y. Then  $h^{-1}(N_{nc}\delta int(N)) \subseteq N_{nc}\gamma int(h^{-1}(N))$ .

(vi)  $\Rightarrow$  (vii) Let *L* be any subset of *Y*. Then h(L) is a subset of *Z*. By (vi), we obtain that  $h^{-1}(N_{nc}\delta int(h(L))) \subseteq N_{nc}\gamma int(h^{-1}(h(L)))$ . Hence  $h^{-1}(N_{nc}\delta int(h(L))) \subseteq N_{nc}\gamma int(L)$ . Which implies that  $N_{nc}\delta int(h(L)) \subseteq h(N_{nc}\gamma int(L))$ .

(vii)  $\Rightarrow$  (i) Let  $p \in Y$  and N be any  $N_{nc}ros$  of Z containing h(p). Then  $p \in h^{-1}(N)$ and  $h^{-1}(N)$  is a subset of Y. By (vii), we get  $N_{nc}\delta int(h(h^{-1}(N))) \subseteq h(N_{nc}\gamma int(h^{-1}(N)))$ implies that  $N_{nc}\delta int(N) \subseteq h(N_{nc}\gamma int(h^{-1}(N)))$ . Since N is  $N_{nc}ros$  and hence N is  $N_{nc}\delta os$ , then  $N \subseteq h(N_{nc}\gamma int(h^{-1}(N)))$  this implies that  $h^{-1}(N) \subseteq N_{nc}\gamma int(h^{-1}(N))$ . Therefore,  $h^{-1}(N)$  is  $N_{nc}\gamma os$  in Y which contains p and clearly  $h(h^{-1}(N)) \subseteq N$ . Hence, by Theorem 3.9, h is  $N_{nc}a\gamma Cts$ . **Corollary 3.12.** Let  $(Y, N_{nc}\Gamma)$  be any  $N_{nc}ts$ . Let L be an  $N_{nc}s$  in  $(Y, N_{nc}\Gamma)$  is  $N_{nc}\beta os$  if and only if  $N_{nc}cl(L)$  is  $N_{nc}rcs$ .

**Theorem 3.13.** For a function  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$ , then the properties are equivalent.

- (i) h is  $N_{nc}a\gamma Cts$ .
- (ii)  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}cl(N))$ , for each  $N_{nc}\gamma os N$  of Z.
- (iii)  $h^{-1}(N_{nc}int(L)) \subseteq N_{nc}\gamma int(h^{-1}(L))$ , for each  $N_{nc}\gamma cs \ L$  of Z.
- (iv)  $h^{-1}(N_{nc}int(L)) \subseteq N_{nc}\gamma int(h^{-1}(L))$ , for each  $N_{nc}Scs L$  of Z.
- (v)  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}cl(N))$ , for each  $N_{nc}Sos N$  of Z.

*Proof.* (i)  $\Rightarrow$  (ii) Let N be any  $N_{nc}\gamma os$  of Z. It follows from Corollary 3.12, that  $N_{nc}cl(N)$  is  $N_{nc}rcs$  in Z. Since h is  $N_{nc}a\gamma Cts$ . Then by Theorem 3.10,  $h^{-1}(N_{nc}cl(N))$  is  $N_{nc}\gamma cs$  in Y. Therefore, we obtain  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}cl(N))$ .

(ii)  $\Leftrightarrow$  (iii) Let L be any  $N_{nc}\gamma cs$  of Z. Then  $Z \setminus L$  is  $N_{nc}\gamma os$  of Z and by (ii), we have  $N_{nc}\gamma cl(h^{-1}(Z \setminus L)) \subseteq h^{-1}(N_{nc}cl(Z \setminus L)) \Leftrightarrow N_{nc}\gamma cl(Y \setminus h^{-1}(L)) \subseteq h^{-1}(Z \setminus N_{nc}int(L)) \Leftrightarrow Y \setminus N_{nc}\gamma int(h^{-1}(L)) \subseteq Y \setminus h^{-1}(N_{nc}int(L))$ . Therefore,  $h^{-1}(N_{nc}int(L)) \subseteq N_{nc}\gamma int(h^{-1}(L))$ . (iii)  $\Rightarrow$  (iv) This is obvious since every  $N_{nc}Scs$  is  $N_{nc}\gamma cs$ .

(iv)  $\Rightarrow$  (v) Let N be any  $N_{nc}Sos$  of Z. Then  $Z \setminus N$  is  $N_{nc}Scs$  and by (iv), we have  $h^{-1}(N_{nc}int(Z\setminus N)) \subseteq N_{nc}\gamma int(h^{-1}(Z\setminus N)) \Leftrightarrow h^{-1}(Z\setminus N_{nc}cl(N)) \subseteq N_{nc}\gamma int(Y\setminus h^{-1}(N)) \Leftrightarrow Y \setminus h^{-1}(N_{nc}cl(N)) \subseteq Y \setminus N_{nc}\gamma cl (h^{-1}(N))$ . Therefore,  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}cl(N))$ .

 $(\mathbf{v}) \Rightarrow (\mathbf{i})$  Let L be any  $N_{nc}rcs$  of Z. Then L is  $N_{nc}Sos$  of Z. By  $(\mathbf{v})$ , we have  $N_{nc}\gamma cl$  $(h^{-1}(L)) \subseteq h^{-1}(N_{nc} cl(L)) = h^{-1}(L)$ . This shows that  $h^{-1}(L)$  is  $N_{nc}\gamma cs$  in Y. Therefore, by Theorem 3.10, h is  $N_{nc}a\gamma Cts$ .

**Corollary 3.14.** Let  $(Y, N_{nc}\Gamma)$  be any  $N_{nc}ts$ . Let L be an  $N_{nc}s$  in  $(Y, N_{nc}\Gamma)$ . Then

- (i)  $L \in N_{nc}SO(Y)$ , then  $N_{nc}Pcl(L) = N_{nc}cl(L)$ .
- (ii)  $L \in N_{nc}\beta O(Y)$ , then  $N_{nc}\alpha cl(L) = N_{nc}cl(L)$ .
- (iii)  $L \in N_{nc}\beta O(Y)$ , then  $N_{nc}\delta cl(L) = N_{nc}cl(L)$ .

**Theorem 3.15.** For a function  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$ , then the statements are equivalent.

- (i) h is  $N_{nc}a\gamma Cts$ .
- (ii)  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}cl(N))$ , for each  $N_{nc}\beta os N$  of Z.
- (iii)  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}\delta cl(N))$ , for each  $N_{nc}\beta os N$  of Z.
- (iv)  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}\gamma cl(N))$ , for each  $N_{nc}Sos N$  of Z.
- (v)  $N_{nc}\gamma cl(h^{-1}(N)) \subseteq h^{-1}(N_{nc}\mathcal{P}cl(N))$ , for each  $N_{nc}\mathcal{S}os N$  of Z.
- *Proof.* (i) ⇒ (ii) Follows from Theorem 3.13 and Corollary 3.14 (ii).
  (ii) ⇒ (iii) This is obvious, since  $N_{nc} \alpha cl(N) \subseteq N_{nc} \delta cl(N)$  in general.
  (iii) ⇒ (iv) and (iv) ⇒ (v) Follows from Corollary 3.14.
  (v) ⇒ (i) Follows from Theorem 3.13 and Corollary 3.14 (i).

**Corollary 3.16.** For a function  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$ , then the statements are equivalent.

- (i) h is  $N_{nc}a\gamma Cts$ .
- (ii)  $h^{-1}(N_{nc}int(N)) \subseteq N_{nc}\gamma int(h^{-1}(N))$ , for each  $N_{nc}\beta cs N$  of Z.
- (iii)  $h^{-1}(N_{nc}\delta int(N)) \subseteq N_{nc}\gamma int(h^{-1}(N))$ , for each  $N_{nc}\beta cs N$  of Z.
- (iv)  $h^{-1}(N_{nc}\gamma int(N)) \subseteq N_{nc}\gamma int(h^{-1}(N))$ , for each  $N_{nc}Scs N$  of Z.
- (v)  $h^{-1}(N_{nc}\mathcal{P}int(N)) \subseteq N_{nc}\gamma int(h^{-1}(N))$ , for each  $N_{nc}\mathcal{S}cs N$  of Z.

**Theorem 3.17.** A function  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$  is  $N_{nc}a\gamma Cts$  if and only if  $h^{-1}(N) \subseteq N_{nc}\gamma int(h^{-1}(N_{nc}int(N_{nc}cl(N))))$  for each  $N_{nc}\mathcal{P}os N$  of Z.

*Proof.* Necessity. Let N be any  $N_{nc}\mathcal{P}os$  of Z. Then  $N \subseteq N_{nc}int(N_{nc}cl(N))$  and  $N_{nc}int(N_{nc}cl(N))$  is  $N_{nc}ros$  in Z. Since h is  $N_{nc}a\gamma Cts$ , by Theorem 3.10,  $h^{-1}(N_{nc}int(N_{nc}cl(N)))$  is  $N_{nc}\gamma os$  in Y and hence we obtain that  $h^{-1}(N) \subseteq h^{-1}(N_{nc}int(N_{nc}cl(N))) = N_{nc}\gamma int(h^{-1}(N_{nc}int(N_{nc}cl(N))))$ .

Sufficiency. Let N be any  $N_{nc}ros$  of Z. Then N is  $N_{nc}\mathcal{P}os$  of Z. By hypothesis, we have  $h^{-1}(N) \subseteq N_{nc}\gamma int(h^{-1}(N_{nc}int(N_{nc}cl(N)))) = N_{nc}\gamma int(h^{-1}(N))$ . Therefore,  $h^{-1}(N)$  is  $N_{nc}\gamma os$  in Y and hence by Theorem 3.10, h is  $N_{nc}a\gamma Cts$ .

**Corollary 3.18.** A function  $h : (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$  is  $N_{nc}a\gamma Cts$  if and only if  $h^{-1}(N) \subseteq N_{nc}\gamma int(h^{-1}(N_{nc}\mathcal{S} cl(N)))$  for each  $N_{nc}\mathcal{P}os N$  of Z.

**Corollary 3.19.** A function  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$  is  $N_{nc}a\gamma Cts$  if and only if  $N_{nc}\gamma cl(h^{-1}(N_{nc}cl(N_{nc}int(L)))) \subseteq h^{-1}(L)$  for each  $N_{nc}\mathcal{P}cs L$  of Z.

**Corollary 3.20.** A function  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$  is  $N_{nc}a\gamma Cts$  if and only if  $N_{nc}\gamma cl(h^{-1}(N_{nc}Sint(L))) \subseteq h^{-1}(L)$  for each  $N_{nc}\mathcal{P}cs L$  of Z.

**Theorem 3.21.** For a function  $h : (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$ , then the statements are equivalent.

- (i) h is  $N_{nc}a\gamma Cts$ .
- (ii) For each neighborhood N of h(p),  $p \in N_{nc}\gamma int(h^{-1}(N_{nc}\mathcal{S}cl(N)))$ .
- (iii) For each neighborhood N of h(p),  $p \in N_{nc}\gamma int(h^{-1}(N_{nc}int(N_{nc}cl(N))))$ .

*Proof.* Follows from Theorem 3.17 and Corollary 3.18.

**Theorem 3.22.** Let  $h : (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$  is an  $N_{nc}a\gamma Cts$  function and Let N be any open subset of Z. If  $p \in N_{nc}\gamma cl(h^{-1}(N)) \setminus h^{-1}(N)$ , then  $h(p) \in N_{nc}\gamma cl(N)$ .

*Proof.* Let  $p \in Y$  be such that  $p \in N_{nc}\gamma cl(h^{-1}(N)) \setminus h^{-1}(N)$  and suppose  $h(p) \notin N_{nc}\gamma cl(N)$ . Then there exists a  $N_{nc}\gamma os \ H \subseteq h(p) \ni H \cap N = \emptyset$ . Then  $N_{nc}cl(H) \cap N = \emptyset$  implies  $N_{nc}int(N_{nc}cl(H)) \cap N = \emptyset$  and  $N_{nc}int(N_{nc}cl(H))$  is  $N_{nc}ros$ . Since h is  $N_{nc}a\gamma Cts$ , by Theorem 3.9, there exists a  $N_{nc}\gamma os \ L$  in Y containing  $p \ni h(L) \subseteq N_{nc}int(N_{nc}cl(H))$ . Therefore,  $h(L) \cap N = \emptyset$ . However, since  $p \in N_{nc}\gamma cl(h^{-1}(N))$ ,  $L \cap h^{-1}(N) \neq \emptyset$  for every  $N_{nc}\gamma os \ L$  in Y containing p, so that  $h(L) \cap N \neq \emptyset$ . We have a contradiction. It follows that  $h(p) \in N_{nc}\gamma cl(N)$ . □

**Theorem 3.23.** If  $h : (Y_1, N_{nc}\Gamma) \to (Y_2, N_{nc}\Psi)$  is  $N_{nc}a\gamma Cts$  and  $h' : (Y_2, N_{nc}\Psi) \to (Y_3, N_{nc}\Phi)$  is  $N_{nc}Cts$  and open. Then the composition function  $h' \circ h : (Y_1, N_{nc}\Gamma) \to (Y_3, N_{nc}\Phi)$  is  $N_{nc}a\gamma Cts$ .

*Proof.* Let  $p \in Y_1$  and N be a  $N_{nc}os$  of  $Y_3$  containing h'(h(p)). Since h' is  $N_{nc}Cts$ ,  $h'^{-1}(N)$  is a  $N_{nc}os$  of  $Y_2$  containing h(p). Since h is  $N_{nc}a\gamma Cts$ ,  $\exists$  a  $N_{nc}\gamma os$  L of  $Y_1$  containing  $p \ni h(L) \subseteq N_{nc}int(N_{nc}cl(h'^{-1}(N)))$ . Also, since h' is  $N_{nc}Cts$ , then we obtain  $(h' \circ h)(L) \subseteq h'(N_{nc}int(h'^{-1}(N_{nc}cl(N))))$ . Since h' is open, we obtain  $(h' \circ h)(L) \subseteq N_{nc}int(N_{nc}cl(N))$ . Therefore,  $h' \circ h$  is  $N_{nc}a\gamma Cts$ . □

**Definition 3.24.** Let  $(Y, N_{nc}\Gamma)$  be any  $N_{nc}ts$ , then Y is said to be N-neutrosophic crisp semiregular (briefly,  $N_{nc}Sr$ ) function if for any  $N_{nc}os L$  of Y and each  $N_{nc}p$ ,  $p \in L$ , there exists a  $N_{nc}ros N$  of  $Y \ni p \in N \subseteq L$ .

**Theorem 3.25.** If  $h: (Y, N_{nc}\Gamma) \to (Z, N_{nc}\Psi)$  is a  $N_{nc}a\gamma Cts$  function and Z is  $N_{nc}Sr$ . Then h is  $N_{nc}\gamma Cts$ .

*Proof.* Let  $p \in Y$  and Let M be any  $N_{nc}os$  of Z containing h(p). By  $N_{nc}Sr$  function of Z, there exists a  $N_{nc}ros G$  of  $Z \ni h(p) \in G \subseteq M$ . Since h is  $N_{nc}a\gamma Cts$ . By Theorem 3.9, there exists a  $N_{nc}\gamma os L$  of Y containing  $p \ni h(L) \subseteq G \subseteq M$ . Therefore, h is  $N_{nc}\gamma Cts$ .

#### 4 Conclusion

We have introduced N-neutrosophic crisp almost  $\gamma$ -continuous functions in a N-neutrosophic crisp  $\gamma$ -open sets via topological spaces. Also, we have established some properties and results of almost  $\gamma$ -continuous function in N-neutrosophic crisp topological spaces. Finally, we study some relation between almost  $\gamma$ -continuous function and  $\gamma$ -continuous function in N-neutrosophic crisp topological spaces as well as their near open sets such as semi-open set, pre-open set and  $\beta$ -open set.

By using N-neutrosophic crisp  $\gamma$ -open set, the notions can be extend to N-neutrosophic crisp almost contra  $\gamma$ -continuous functions, N-neutrosophic crisp  $\gamma$  open mappings, N-neutrosophic crisp  $\gamma$  closed mappings, N-neutro-sophic crisp  $\gamma$  homomorphisms and N-neutrosophic crisp  $\gamma$  irresolute functions in N-neutrosophic crisp topological spaces in future. Additionally, the notions can be tried in programming languages like C++, MATLAB, Python, etc. to simplify the results in topology.

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